Exercise 19

Explain why the function is discontinuous at the given number a. Sketch the graph of the function.

$$f(x) = \begin{cases} x+3 & \text{if } x \le -1 \\ & & \\ 2^x & \text{if } x > -1 \end{cases} \qquad a = -1$$

Solution

A graph of the function versus x is shown below.



The function is discontinuous at x = -1 because the left-hand and right-hand limits are not equal there. In other words,

$$\lim_{x \to -1} f(x)$$

does not exist.